

# Steady-State

Fixed-point in the absence of shocks

# Steady-State Recipe

$$1. \bar{A} = 1$$

$$2. \bar{M}C = 1$$

$$3. \bar{R} = \frac{1}{\beta} + \delta - 1$$

$$4. \frac{\bar{K}}{\bar{L}} = \left( \bar{M}C \frac{\alpha \bar{A}}{\bar{R}} \right)^{\frac{1}{1-\alpha}}$$

$$5. \bar{W} = \bar{M}C(1 - \alpha)\bar{A} \left( \frac{\bar{K}}{\bar{L}} \right)^{\alpha}$$

$$6. \frac{\bar{I}}{\bar{L}} = \delta \frac{\bar{K}}{\bar{L}}$$

$$7. \frac{\bar{Y}}{\bar{L}} = \bar{A} \left( \frac{\bar{K}}{\bar{L}} \right)^{\alpha}$$

$$8. \frac{\bar{C}}{\bar{L}} = \frac{\bar{Y}}{\bar{L}} - \frac{\bar{I}}{\bar{L}}$$

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8. Log-utility (determine  $\bar{L}$  analytically): 
$$\bar{L} = \frac{\frac{\gamma}{\psi} \left(\frac{\bar{C}}{\bar{L}}\right)^{-1} \bar{W}}{1 + \frac{\gamma}{\psi} \left(\frac{\bar{C}}{\bar{L}}\right)^{-1} \bar{W}}$$

8. CES-utility (determine  $\bar{L}$  numerically): 
$$\bar{W} \left(\frac{\bar{C}}{\bar{L}}\right)^{-\eta_C} = \frac{\psi}{\gamma} (1 - \bar{L})^{-\eta_L} \bar{L}^{\eta_C}$$

9. Remaining variables: 
$$\bar{C} = \frac{\bar{C}}{\bar{L}} \bar{L}, \quad \bar{I} = \frac{\bar{I}}{\bar{L}} \bar{L}, \quad \bar{K} = \frac{\bar{K}}{\bar{L}} \bar{L}, \quad \bar{Y} = \frac{\bar{Y}}{\bar{L}} \bar{L}$$